

Small positive loops of contactomorphisms

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Contact geometry focuses on the study of odd dimensional manifolds M^{2n+1} which admit a hyperplane distribution $\xi = \ker \alpha$ such that the differential form $\alpha \in \Omega^1(M)$ satisfies $\alpha \wedge d\alpha^n \neq 0$. Those manifolds are locally identical due to Darboux theorem, which provides a local model for α . By contrast, a global criteria related to homotopic properties of distributions classifies compact contact manifolds in two different types: overtwisted and tight.

Appart from doing a review of the previous concepts, in this talk we are going to tackle a problem related to loops of contactomorphism $\Phi: M \times S^1 \rightarrow M$ on overtwisted manifolds. In particular, we are going to prove that if the Hamiltonian of a loop $H = \alpha(\frac{d}{dt}\Phi_t)$ is positive, then it is bounded below by a universal constant which only depends on α .