



DEPARTAMENTO DE  
ANÁLISIS MATEMÁTICO Y  
MATEMÁTICA APLICADA



# SEMINARIO DE MATEMÁTICA APLICADA

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# Existence of a positive solution to a nonlinear scalar field equation with zero mass at infinity

**Abstract:** We establish the existence of a positive solution to the problem

$$-\Delta u + V(x)u = f(u), \quad u \in D^{1,2}(\mathbb{R}^N), \quad (1)$$

for  $N \geq 3$ , when the nonlinearity  $f$  is subcritical at infinity and supercritical near the origin, and the potential  $V$  vanishes at infinity.

For  $V \equiv 0$  this problem was addressed by Berestycki and Lions in their groundbreaking paper published in ARMA in 1983. They called it the *zero mass* case.

Our result includes situations in which problem (1) does not have a ground state. Then, under a suitable decay assumption on the potential  $V$ , we show that it has a positive bound state.

This is joint work with Liliane Maia (University of Brasilia).

**Organizado por el Instituto de Matemática Interdisciplinar (IMI), el grupo CADEDIF y el Departamento de Análisis Matemático y Matemática Aplicada**

**Fecha: Martes, 16 de octubre de 2018**

**Hora: 12:00 horas**

**Lugar: Aula 209 (Seminario Alberto Dou)**

**Facultad de CC Matemáticas, UCM**